FINAL JEE-MAIN EXAMINATION - SEPTEMBER, 2020 (Held On Friday 04 <sup>th</sup> SEPTEMBER, 2020) TIME : 3 PM to 6 PM			
	MATHEMATICS		TEST PAPER WITH SOLUTION
1.	The function $f(x) = \begin{cases} \frac{\pi}{4} + \tan^{-1} x,  x  \le 1\\ \frac{1}{2}( x -1),  x  > 1 \end{cases}$ is :	2.	Let $\bigcup_{i=1}^{50} X_i = \bigcup_{i=1}^{n} Y_i = T$ , where each $X_i$ contains 10 elements and each $Y_i$ contains 5 elements. If each element of the set T is an element of exactly 20 of sets $X_i$ 's and exactly 6 of sets $Y_i$ 's,
	<ol> <li>(1) continuous on R-{1} and differentiable on R - {-1, 1}.</li> <li>(2) both continuous and differentiable on R - {-1}.</li> <li>(3) continuous on R - {-1} and differentiable on R - {-1, 1}.</li> <li>(4) both continuous and differentiable on R -{1}</li> <li>Official Ans. by NTA (1)</li> </ol>	Sol.	then n is equal to : (1) 45 (2) 15 (3) 50 (4) 30 <b>Official Ans. by NTA (4)</b> $n(X_i) = 10. \bigcup_{i=1}^{50} X_i = T, \Rightarrow n (T) = 500$ each element of T belongs to exactly 20 elements of $X_i \Rightarrow \frac{500}{20} = 25$ distinct elements
Sol.	$f(\mathbf{x}) = \begin{cases} \frac{\pi}{4} + \tan^{-1} \mathbf{x} & ,  \mathbf{x} \in (-\infty, -1] \cup [1, \infty) \\ -\frac{(\mathbf{x}+1)}{2} & ,  \mathbf{x} \in (-1, 0] \\ \frac{\mathbf{x}-1}{2} & ,  \mathbf{x} \in (0, 1) \end{cases}$	3.	so $\frac{5n}{6} = 25 \Rightarrow n = 30$ Let $\lambda \neq 0$ be in R. If $\alpha$ and $\beta$ are the roots of the equation, $x^2 - x + 2\lambda = 0$ and $\alpha$ and $\gamma$ are the roots of the equation, $3x^2 - 10x + 27\lambda = 0$ , then $\frac{\beta\gamma}{\lambda}$ is equal to :
	for continuity at $x = -1$ L.H.L. $= \frac{\pi}{4} - \frac{\pi}{4} = 0$ R.H.L. $= 0$ so, continuous at $x = -1$ for continuity at $x = 1$ L.H.L. $= 0$	Sol.	(1) 36 (2) 27 (3) 9 (4) 18 Official Ans. by NTA (4)
	R.H.L. = $\frac{\pi}{4} + \frac{\pi}{4} = \frac{\pi}{2}$ so, not continuous at x = 1 For differentiability at x = -1 L.H.D. = $\frac{1}{1+1} = \frac{1}{2}$ R.H.D. = $-\frac{1}{2}$ so, non differentiable at x = -1		$\gamma - \beta = \frac{7}{3},$ $\frac{\gamma}{\beta} = \frac{9}{2} \Rightarrow \gamma = \frac{9}{2}\beta = \frac{9}{2} \times \frac{2}{3} \Rightarrow \gamma = 3$ $\frac{9}{2}\beta - \beta = \frac{7}{3}$ $\frac{9}{2}\beta = \frac{7}{3} \Rightarrow \beta = \frac{2}{3}$

$$\alpha = 1 - \frac{2}{3} = \frac{1}{3}$$
$$2\lambda = \frac{2}{9} \Rightarrow \lambda = \frac{1}{9}$$
$$\frac{\beta\gamma}{\lambda} = \frac{\frac{2}{3} \times 3}{\frac{1}{9}} = 18$$

4. The solution of the differential equation

$$\frac{dy}{dx} - \frac{y + 3x}{\log_e(y + 3x)} + 3 = 0$$
 is :-

(where C is a constant of integration.) (1) x-2 log<sub>e</sub>(y+3x)=C (2) x-log<sub>e</sub>(y+3x)=C (3) x- $\frac{1}{2}(\log_{e}(y+3x))^{2} = C$ (4) y + 3x- $\frac{1}{2}(\log_{e}x)^{2} = C$ 

**Official Ans. by NTA (3)** Sol. ln(y + 3x) = z (let)

$$\frac{1}{y+3x} \cdot \left(\frac{dy}{dx} + 3\right) = \frac{dz}{dx} \qquad ..(1)$$

$$\frac{dy}{dx} + 3 = \frac{y + 3x}{\ell n(y + 3x)} \quad (given)$$

$$\frac{dz}{dx} = \frac{1}{z}$$

$$\Rightarrow z \, dz = dx \Rightarrow \frac{z^2}{2} = x + C$$

$$\Rightarrow \frac{1}{2}\ell n^2(y + 3x) = x + C$$

$$\Rightarrow x - \frac{1}{2} (\ell n(y + 3x))^2 = C$$

- 5. Let  $a_1$ ,  $a_2$ ...,  $a_n$  be a given A.P. whose common difference is an integer and  $S_n = a_1 + a_2 + ..+ a_n$ . If  $a_1 = 1$ ,  $a_n = 300$  and  $15 \le n \le 50$ , then the ordered pair ( $S_{n-4}, a_{n-4}$ ) is equal to : (1) (2480, 249) (2) (2490, 249) (3) (2490, 248) (4) (2480, 248) **Official Ans. by NTA (3)**
- Sol.  $\mathbf{a}_{\mathbf{n}} = \mathbf{a}_1 + (\mathbf{n} - 1)\mathbf{d}$  $\Rightarrow 300 = 1 + (n - 1) d$  $\Rightarrow$  (n - 1)d = 299 = 13 × 23 since,  $n \in [15, 50]$  $\therefore$  n = 24 and d = 13  $a_{n-4} = a_{20} = 1 + 19 \times 13 = 248$  $\Rightarrow a_{n-4} = 248$  $S_{n-4} = \frac{20}{2} \{1 + 248\} = 2490$ The distance of the point (1, -2, 3) from the 6. plane x-y+z = 5 measured parallel to the line  $\frac{x}{2} = \frac{y}{3} = \frac{z}{-6}$  is : (2) 1 (3)  $\frac{1}{7}$  (4)  $\frac{7}{5}$ (1) 7Official Ans. by NTA (2) **Sol.** equation of line parallel to  $\frac{x}{2} = \frac{y}{3} = \frac{z}{-6}$  passes through (1, -2, 3) is  $\frac{x-1}{2} = \frac{y+2}{3} = \frac{z-3}{-6} = r$ x = 2r + 1y = 3r - 2, z = -6r + 32r + 1 - 3r + 2 - 6r + 3 = 5So -7r + 1 = 0 $\Rightarrow$  $r = \frac{1}{7}$  $x = \frac{9}{7}, y = \frac{-11}{7}, z = \frac{15}{7}$ Distance is =  $\sqrt{\left(\frac{9}{7}-1\right)^2 + \left(2-\frac{11}{7}\right)^2 + \left(3-\frac{15}{7}\right)^2}$  $=\sqrt{\left(\frac{2}{7}\right)^2 + \left(\frac{3}{7}\right)^2 + \left(\frac{6}{7}\right)^2}$  $=\frac{1}{7}\sqrt{4+9+36}$  $=\frac{1}{7}\sqrt{49} = 1$

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7. Let 
$$f: (0, \infty) \rightarrow (0, \infty)$$
 be a differentiable function such that  $f(1) = e$  and  

$$\lim_{i \to x} \frac{t^2 f^2(x) - x^2 f^2(t)}{t - x} = 0$$
If  $f(x) = 1$ , then x is equal to :  
(1)  $2e$  (2)  $\frac{1}{2e}$  (3)  $e$  (4)  $\frac{1}{e}$   
Official Ans. by NTA (4)  
Sol.  $L = \lim_{t \to x} \frac{t^2 f^2(x) - x^2 f^2(t)}{t - x}$   
using L.H. rule  
 $L = \lim_{t \to x} \frac{2t f^2(x) - x^2 \cdot 2f'(t) \cdot f(t)}{1}$   
 $\Rightarrow L = 2xf(x) (f(x) - x f(x)) = 0 (given)$   
 $\Rightarrow f(x) = xf'(x) \Rightarrow \int \frac{f'(x) dx}{f(x)} = \int \frac{dx}{x}$   
 $\Rightarrow ln f(x)| = ln |x| + C$   
 $\because f(1) = e, x > 0, f(x) > 0$   
 $\Rightarrow f(x) = ex, \quad \text{if } f(x) = 1 \Rightarrow x = \frac{1}{e}$   
8. If the system of equations  
 $x + y + z = 2$   
 $2x + 4y - z = 6$   
 $3x + 2y + \lambda z = \mu$   
has infinitely many solutions, then :  
(1)  $\lambda - 2\mu = -5$  (2)  $2\lambda - \mu = 5$   
(3)  $2\lambda + \mu = 14$  (4)  $\lambda + 2\mu = 14$   
Official Ans. by NTA (3)  
Sol. For infinite solutions  
 $\Delta = \Delta_x = \Delta_y = \Delta_z = 0$   
Now  $\Delta = 0 \Rightarrow \begin{vmatrix} 1 & 1 & 1 \\ 2 & 4 & -1 \\ 3 & 2 & \lambda \end{vmatrix} = 0$   
 $\Rightarrow \lambda = \frac{9}{2}$   
 $\Delta_{x=0} \Rightarrow \begin{vmatrix} 2 & 1 & 1 \\ 6 & 4 & -1 \\ \mu & 2 & -\frac{9}{2} \end{vmatrix}$ 

 $\Rightarrow \mu = 5$ For  $\lambda = \frac{9}{2}$  &  $\mu = 5$ ,  $\Delta_y = \Delta_z = 0$ Now check option  $2\lambda + \mu = 14$ 9. The minimum value of  $2^{sinx} + 2^{cosx}$  is :-(1)  $2^{1-\frac{1}{\sqrt{2}}}$ (2)  $2^{-1+\sqrt{2}}$ (4)  $2^{-1+\frac{1}{\sqrt{2}}}$ (3)  $2^{1-\sqrt{2}}$ Official Ans. by NTA (1) **Sol.** Usnign  $AM \ge GM$  $\Rightarrow \frac{2^{\sin x} + 2^{\cos x}}{2} \ge \sqrt{2^{\sin x} \cdot 2^{\cos x}}$  $\Rightarrow 2^{\sin x} + 2^{\cos x} \ge 2^{1 + \left(\frac{\sin x + \cos x}{2}\right)}$  $\Rightarrow \min(2^{\sin x} + 2^{\cos x}) = 2^{1 - \frac{1}{\sqrt{2}}}$ **10.**  $\int_{\pi/2}^{\pi/3} \tan^3 x \cdot \sin^2 3x (2 \sec^2 x \cdot \sin^2 3x + 3 \tan x \cdot \sin 6x) dx$ is equal to : (1)  $\frac{9}{2}$  (2)  $-\frac{1}{9}$  (3)  $-\frac{1}{18}$  (4)  $\frac{7}{18}$ Official Ans. by NTA (3) **Sol.** I =  $\int_{-\pi/3}^{\pi/3} ((2 \tan^3 x \cdot \sec^2 x \cdot \sin^4 3x) + (3 \tan^4 x \cdot \sin^3 3x \cdot \cos 3x)) dx$  $\Rightarrow I = \frac{1}{2} \int_{\frac{\pi}{2}}^{\frac{\pi}{3}} d((\sin 3x)^4 (\tan x)^4)$  $\Rightarrow I = ((\sin 3x)^4 (\tan x)^4)_{\pi/6}^{\pi/3}$  $\Rightarrow$  I =  $-\frac{1}{18}$ The circle passing through the intersection of 11. the circles,  $x^2 + y^2 - 6x = 0$  and  $x^2 + y^2 - 4y = 0$ , having its centre on the line, 2x - 3y + 12 = 0, also passes through the point : (1) (1, -3)(2) (-1, 3)(4) (-3, 6)(3) (-3, 1)Official Ans. by NTA (4) Sol. Let S be the circle pasing through point of interpretion of C P C

intersection of 
$$S_1 \approx S_2$$
  
 $\therefore S = S_1 + \lambda S_2 = 0$   
 $\Rightarrow S : (x^2 + y^2 - 6x) + \lambda (x^2 + y^2 - 4y) = 0$ 

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$$\Rightarrow S : x^{2} + y^{2} - \left(\frac{6}{1+\lambda}\right)x - \left(\frac{4\lambda}{1+\lambda}\right)y = 0 \dots (1)$$
Centre  $\left(\frac{3}{1+\lambda}, \frac{2\lambda}{1+\lambda}\right)$  lies on  
 $2x - 3y + 12 = 0 \Rightarrow \lambda = -3$   
put in (1)  $\Rightarrow S : x^{2} + y^{2} + 3x - 6y = 0$   
Now check options point (-3, 6)  
lies on S.  
12. The angle of elevation of a cloud C from a point  
P, 200 m above a still lake is 30°. If the angle  
of depression of the image of C in the lake from  
the point P is 60°, then PC (in m) is equal to :  
(1) 400 (2) 400  $\sqrt{3}$   
(3) 100 (4) 200  $\sqrt{3}$   
Official Ans. by NTA (1)  
Sol. Let PA = x  
For  $\Delta APC$   
 $AC = \frac{PA}{\sqrt{3}} = \frac{x}{\sqrt{3}}$  200  
 $AC^{1} = AB + BC^{1}$   
 $AC^{1} = AB + BC$   
 $AC^{1} = 400 + \frac{x}{\sqrt{3}}$   
From  $\Delta C^{1}PA$  :  $AC^{1} = \sqrt{3} PA$   
 $\Rightarrow \left(400 + \frac{x}{\sqrt{3}}\right) = \sqrt{3}x \Rightarrow x = (200)(\sqrt{3})$   
from  $\Delta APC$  :  $PC = \frac{2x}{\sqrt{3}} \Rightarrow PC = 400$   
13. If a and b are real numbers such that  
 $(2 + \alpha)^{4} = a + b\alpha$ , where  $\alpha = \frac{-1 + i\sqrt{3}}{2}$ , then  
 $a + b$  is equal to :  
(1) 57 (2) 33 (3) 24 (4) 9  
Official Ans. by NTA (4)  
Sol.  $\alpha = \omega$  ( $\omega^{3} = 1$ )  
 $\Rightarrow (2 + \omega)^{4} = a + b\omega$   
 $\Rightarrow 2^{4} + 4.2^{3} \omega + 6.2^{2}\omega^{3} + 4.2 \cdot \omega^{3} + \omega^{4}$   
 $= a + b\omega$   
 $\Rightarrow 24 + 4.24 \omega^{2} + 3\omega = a + b\omega$   
 $\Rightarrow -24\omega + 33\omega = a + b\omega$   
 $\Rightarrow -24\omega + 33\omega = a + b\omega$   
 $\Rightarrow -24\omega + 33\omega = a + b\omega$   
 $\Rightarrow a = 0, b = 9$ 

14. In a game two players A and B take turns in throwing a pair of fair dice starting with player A and total of scores on the two dice, in each throw is noted. A wins the game if he throws a total of 6 before B throws a total of 7 and B wins the game if he throws a total of 7 before A throws a total of six The game stops as soon as either of the players wins. The probability of A winning the game is :

(1) 
$$\frac{31}{61}$$
 (2)  $\frac{5}{6}$ 

(3) 
$$\frac{5}{31}$$
 (4)  $\frac{30}{61}$ 

Official Ans. by NTA (4)

Sol. 
$$P(6) = \frac{1}{6}$$
,  $P(7) = \frac{5}{36}$   
 $P(A) = W + FFW + FFFFW + .....$   
 $= \frac{1}{6} + \frac{5}{6} \times \frac{31}{36} \times \frac{1}{6} + \left(\frac{5}{6}\right)^2 \left(\frac{31}{36}\right)^2 \frac{1}{6} + ...$   
 $= \frac{\frac{1}{6}}{1 - \frac{155}{216}} = \frac{36}{61}$ 

**15.** Let x = 4 be a directrix to an ellipse whose centre is at the origin and its eccentricity is  $\frac{1}{2}$ .

If P (1,  $\beta$ ),  $\beta > 0$  is a point on this ellipse, then the equation of the normal to it at P is :-

(1) 7x - 4y = 1 (2) 4x - 2y = 1(3) 4x - 3y = 2 (4) 8x - 2y = 5Official Ans. by NTA (2)

**Sol.** Ellipse :  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ 

directrix : 
$$x = \frac{a}{e} = 4$$
 &  $e = \frac{1}{2}$   
 $\Rightarrow a = 2$  &  $b^2 = a^2 (1-e^2) = 3$   
 $\Rightarrow$  Ellipse is  $\frac{x^2}{4} + \frac{y^2}{3} = 1$   
P is  $\left(1, \frac{3}{2}\right)$ 

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Normal is : 
$$\frac{4x}{1} - \frac{3y}{3/2} = 4 - 3$$

 $\Rightarrow 4x - 2y = 1$ 

- 16. Contrapositive of the statement:'If a function f is differentiable at a, then it is also continuous at a', is :-
  - (1) If a function f is continuous at a, then it is not differentiable at a.
  - (2) If a function f is not continuous at a, then it is differentiable at a.
  - (3) If a function f is not continuous at a, then it is not differentiable at a.
  - (4) If a function f is continuous at a, then it is differentiable at a.

#### Official Ans. by NTA (3)

- Sol. p = function is differentiable at a q = function is continuous at a contrapositive of statement  $p \rightarrow q$  is  $\sim q \rightarrow \sim p$
- 17. The area (in sq. units) of the largest rectangle ABCD whose vertices A and B lie on the x-axis and vertices C and D lie on the parabola, y= x<sup>2</sup> -1 below the x-axis, is :

(1) 
$$\frac{4}{3\sqrt{3}}$$
 (2)  $\frac{1}{3\sqrt{3}}$  (3)  $\frac{4}{3}$  (4)  $\frac{2}{3\sqrt{3}}$ 

#### Official Ans. by NTA (1)

**Sol.** Area (A) =  $2t \cdot (1 - t^2)$ 

$$(0 < t < 1)$$

$$A = 2t - 2t^{3}$$

$$\frac{dA}{dt} = 2 - 6t^{2}$$

$$t = \frac{1}{\sqrt{3}}$$

$$(-t, t^{2} - 1)$$

18. If for some positive integer n, the coefficients of three consecutive terms in the binomial expansion of  $(1+x)^{n+5}$  are in the ratio 5:10:14, then the largest coefficient in this expansion is :-

(1) 792 (2) 252 (3) 462 (4) 330

Official Ans. by NTA (3)

**Sol.** Let 
$$n + 5 = N$$

$$N_{C_{r+1}}: N_{C_r}: N_{C_{r+1}} = 5: 10: 14$$

$$\Rightarrow \frac{N_{C_r}}{N_{C_{r-1}}} = \frac{N+1-r}{r} = 2$$

$$\frac{N_{C_{r+1}}}{N_{C_r}} = \frac{N-r}{r+1} = \frac{7}{5}$$
$$\implies r = 4, N = 11$$

$$\Rightarrow (1 + x)^{11}$$

Largest coefficient =  ${}^{11}C_6 = 462$ 

**19.** If the perpendicular bisector of the line segment joining the points P (1, 4) and Q (k, 3) has y-intercept equal to -4, then a value of k is :-

(1)  $\sqrt{15}$  (2) -2 (3)  $\sqrt{14}$  (4) -4

Official Ans. by NTA (4)

Slope =  $m = \frac{1}{1-k}$ 

Equation of 
$$\perp^r$$
 bisector is  
 $y + 4 = (k - 1) (x - 0)$   
 $\Rightarrow y + 4 = x(k - 1)$   
 $\Rightarrow \frac{7}{2} + 4 = \frac{k + 1}{2}(k - 1)$   
 $\Rightarrow \frac{15}{2} = \frac{k^2 - 1}{2} \Rightarrow k^2 = 16 \Rightarrow k = 4, -4$ 

## VIDYAPEETH Sinal JEE -Main Exam September, 2020/04-09-2020/Evening Session

20. Suppose the vectors x<sub>1</sub>, x<sub>2</sub> and x<sub>3</sub> are the solutions of the system of linear equations, Ax = b when the vector b on the right side is equal to b<sub>1</sub>, b<sub>2</sub> and b<sub>3</sub> respectively. If

$$\mathbf{x} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}, \mathbf{x}_2 = \begin{bmatrix} 0 \\ 2 \\ 1 \end{bmatrix}, \mathbf{x}_3 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, \mathbf{b}_1 = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

$$\mathbf{b}_2 = \begin{bmatrix} 0\\2\\0 \end{bmatrix}$$
 and  $\mathbf{b}_3 = \begin{bmatrix} 0\\0\\2 \end{bmatrix}$ , then the determinant of

A is equal to :-

(1)  $\frac{1}{2}$  (2) 4 (3)  $\frac{3}{2}$  (4) 2

Official Ans. by NTA (4)

Sol.  $Ax_1 = b_1$   $Ax_2 = b_2$   $Ax_3 = b_3$  $\Rightarrow |A| \begin{vmatrix} 1 & 0 & 0 \\ 1 & 2 & 0 \\ 1 & 1 & 1 \end{vmatrix} = \begin{vmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{vmatrix}$ 

 $\Rightarrow$  |A| =  $\frac{4}{2}$  = 2

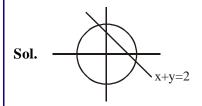
21. A test consists of 6 multiple choice questions, each having 4 alternative answers of which only one is correct. The number of ways, in which a candidate answers all six questions such that exactly four of the answers are correct, is \_\_\_\_

Official Ans. by NTA (135) Sol. Ways =  ${}^{6}C_{4} \cdot 1^{4} \cdot 3^{2}$ 

$$= 15 \times 9$$
  
= 135

22. Let PQ be a diameter of the circle  $x^2+y^2=9$ . If  $\alpha$  and  $\beta$  are the lengths of the perpendiculars from P and Q on the straight line, x + y = 2 respectively, then the maximum value of  $\alpha\beta$  is

Official Ans. by NTA (7)



Let P (
$$3\cos\theta$$
,  $3\sin\theta$ )  
Q ( $-3\cos\theta$ ,  $-3\sin\theta$ )  
 $\Rightarrow \alpha\beta = \frac{1(3\cos\theta + 3\sin\theta)^2 - 41}{2}$   
 $\Rightarrow \alpha\beta = \frac{5 + 9\sin 2\theta}{2} \le 7$ 

23. Let {x} and [x] denote the fractional part of x and the greatest integer ≤ x respectively of a real number x. If ∫<sub>0</sub><sup>n</sup>{x}dx, ∫<sub>0</sub><sup>n</sup>[x]dx and 10(n<sup>2</sup> - n), (n ∈ N, n > 1) are three consecutive terms of a G.P., then n is equal to\_\_\_\_\_Official Ans. by NTA (21)

Sol. 
$$\int_{0}^{n} \{x\} dx = n \int_{0}^{1} \{x\} dx = n \int_{0}^{1} x \, dx = \frac{n}{2}$$
$$\int_{0}^{n} [x] dx = \int_{0}^{n} (x - \{x\}) dx = \frac{n^{2}}{2} - \frac{n}{2}$$
$$\Rightarrow \left(\frac{n^{2} - n}{2}\right)^{2} = \frac{n}{2} \cdot 10 \cdot n(n - 1) \text{ (where } n > 1)$$
$$\Rightarrow \frac{n - 1}{4} = 5 \Rightarrow n = 21$$

24. If  $\vec{a} = 2\hat{i} + \hat{j} + 2\hat{k}$ , then the value of  $|\hat{i} \times (\vec{a} \times \hat{i})|^2 + |\hat{j} \times (\vec{a} \times \hat{j})|^2 + |\hat{k} \times (\vec{a} \times \hat{k})|^2$  is equal to \_\_\_\_\_ Official Ans. by NTA (18)

Sol. 
$$\Sigma |\vec{a} - (\vec{a} \cdot i)i|^2$$
  
 $\Rightarrow \Sigma (|a|^2 + (\vec{a} \cdot i)^2 - 2(\vec{a} \cdot i)^2)$   
 $\Rightarrow 3 |\vec{a}|^2 - \Sigma (\vec{a} \cdot i)^2$   
 $\Rightarrow 2 |\vec{a}|^2$   
 $\Rightarrow 18$ 

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# **VIDYAPEETH** Final JEE -Main Exam September, 2020/04-09-2020/Evening Session

If the variance of the following frequency 25. distribution : Class : 10-20 20-30 30-40 Frequency : 2 2 х is 50, then x is equal to \_\_\_\_ **Official Ans. by NTA (4) Sol.** : Variance is independent of shifting of origin  $\Rightarrow x_i : 15$ 25 35 or -10 0 10  $f_i$ : 2 x 2 2 x 2  $\Rightarrow \quad \text{Variance } (\sigma^2) = \frac{\Sigma x_i^2 f_i}{\Sigma f_i} - (\vec{x})^2$  $\Rightarrow 50 = \frac{200 + 0 + 200}{x + 4} - 0 \qquad \left\{\overline{x} = 0\right\}$ 200 + 50x = 200 + 200 $\Rightarrow$  $\Rightarrow x = 4$